



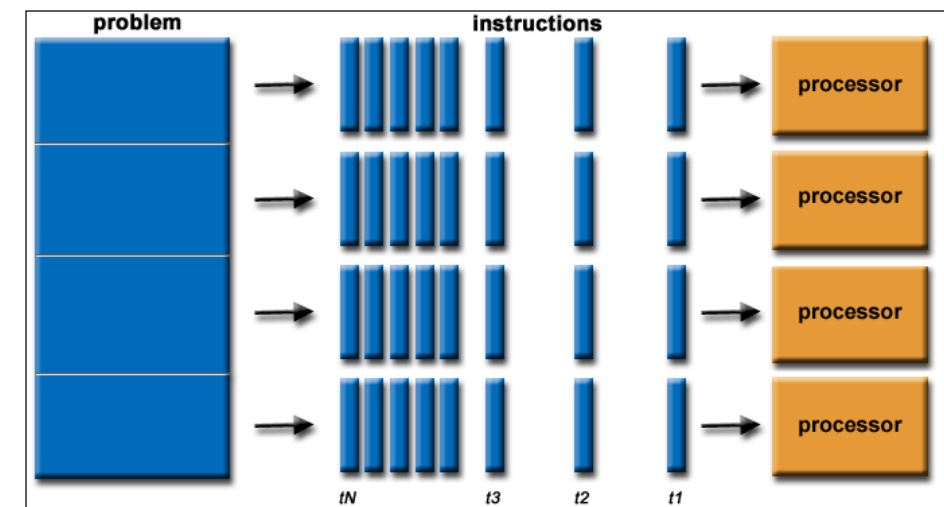
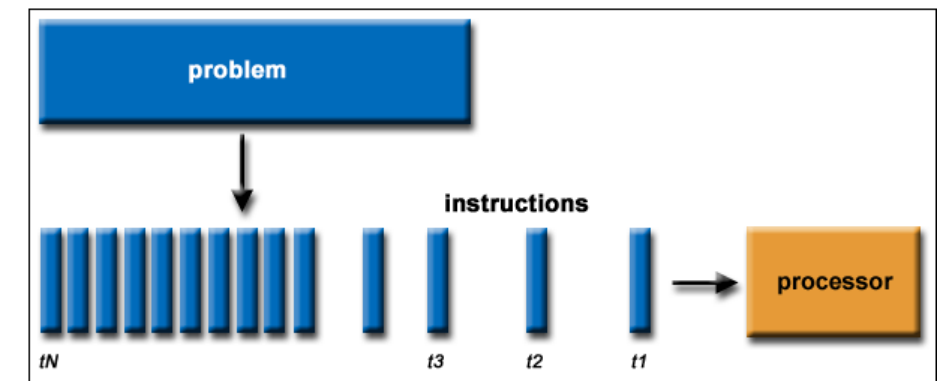
Introduction to parallel Computing

Outline

- Serial vs Parallel programming
- Hardware trends
- Why HPC matters
- HPC Concepts and Terminology
- Amdahl's Law and Scalability
- Parallel programming models
- Communications
- Synchronization
- Load Balancing
- Pseudo-code examples

Serial vs Parallel Programming

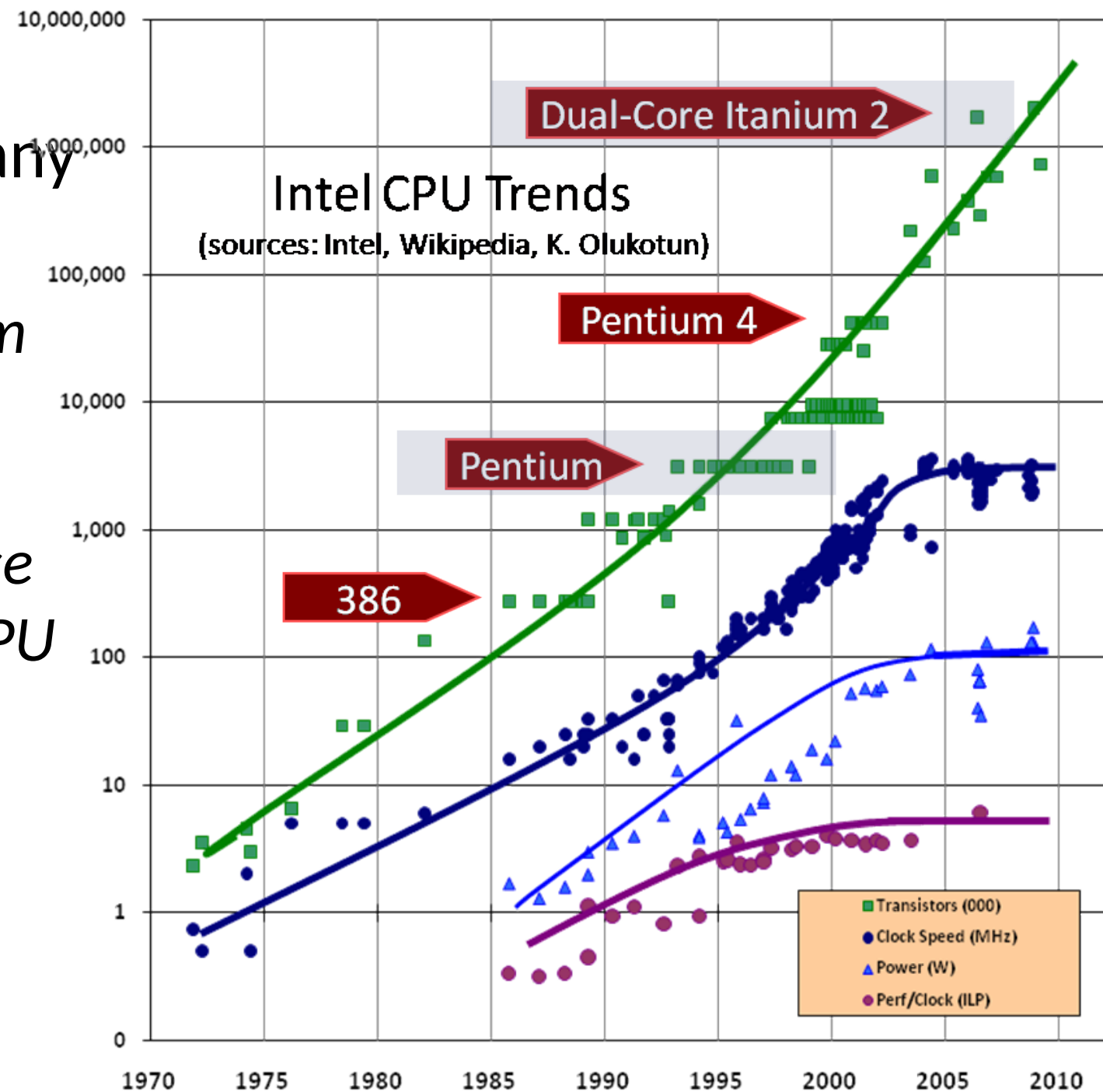
- Traditionally software is written for serial computation
 - A problem is broken into discrete parts
 - Parts (instructions) are executed each at a time (serially)
- In parallel programming more than one processors are used
 - Problem is broken into discrete parts that can be solved **concurrently**
 - Several instructions are executed at a given time **asynchronously**
 - An overall control (syncing) mechanism is needed



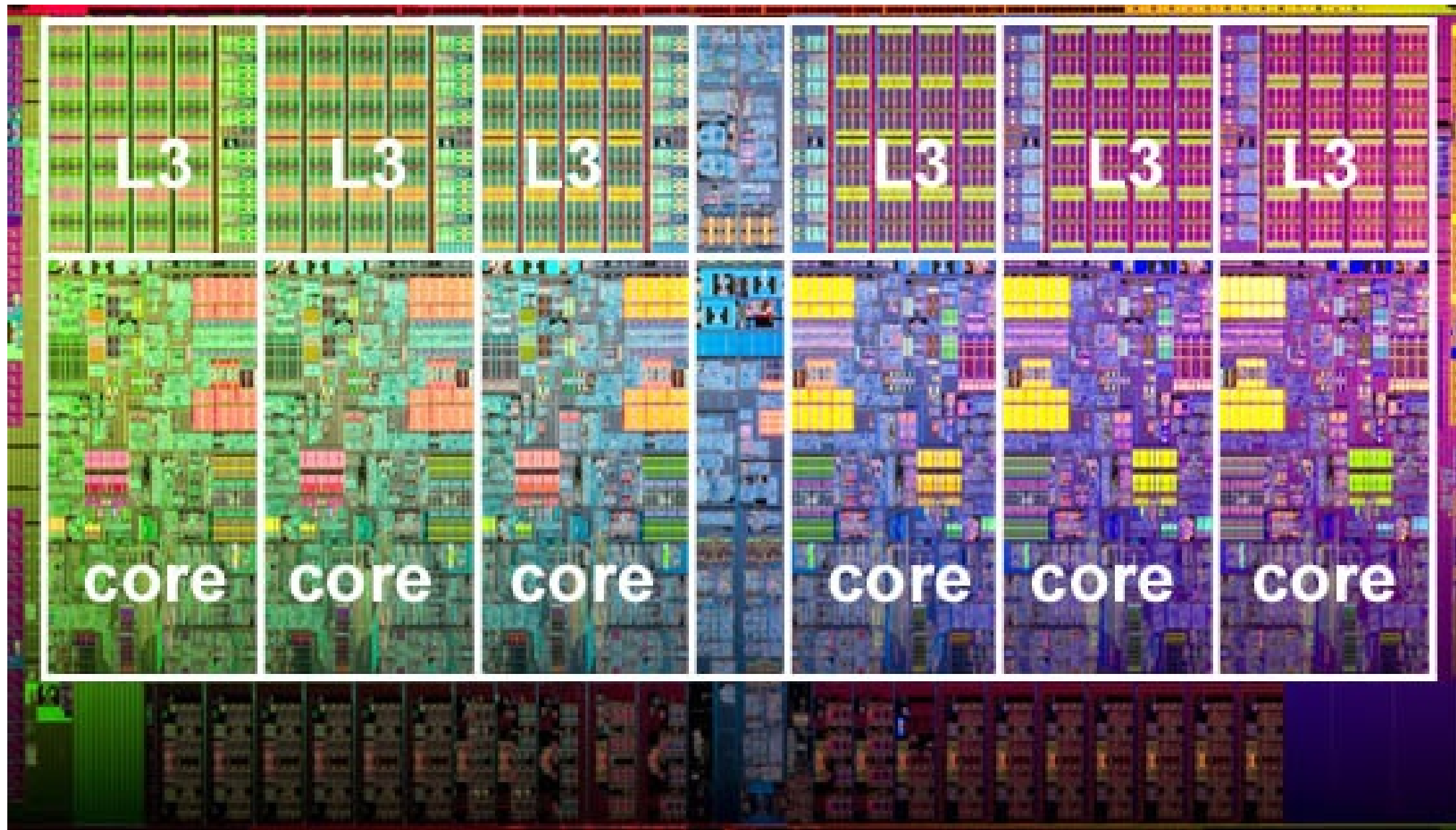
CPU trends

- We are not living in the 90s any more...

“From 2007 to 2011, maximum CPU clock speed (with Turbo Mode enabled) rose from 2.93GHz to 3.9GHz, an increase of 33%. From 1994 to 1998, CPU clock speeds rose by 300%.”

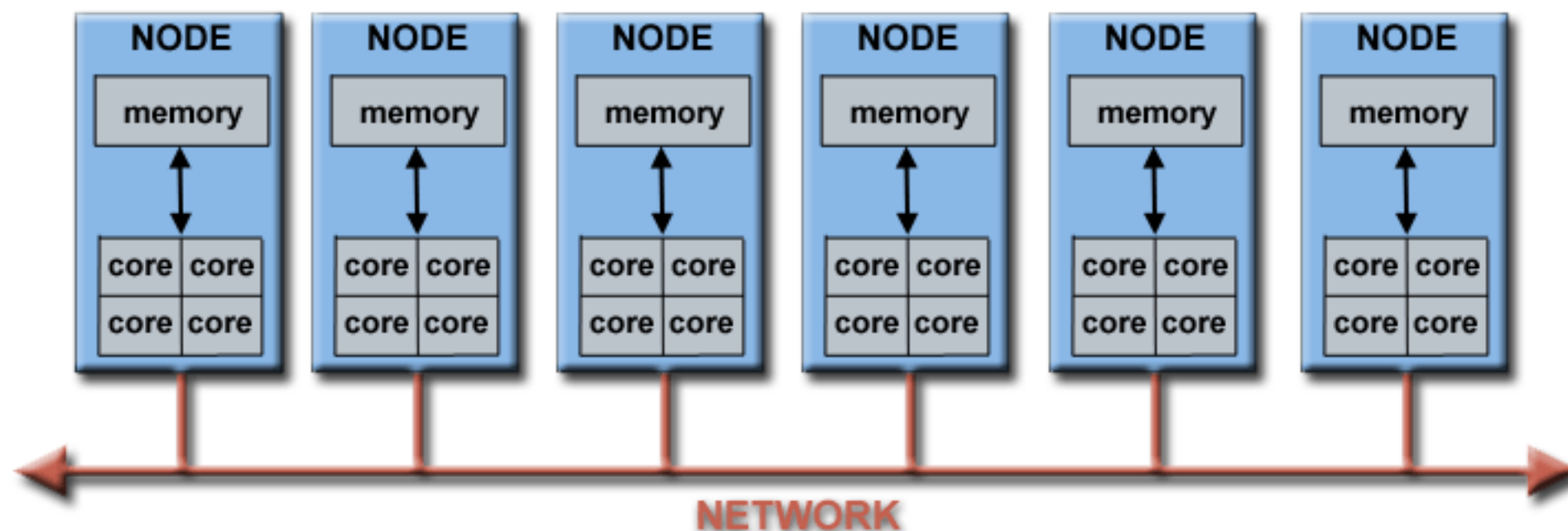


Hardware nowadays **is** designed for parallel computing



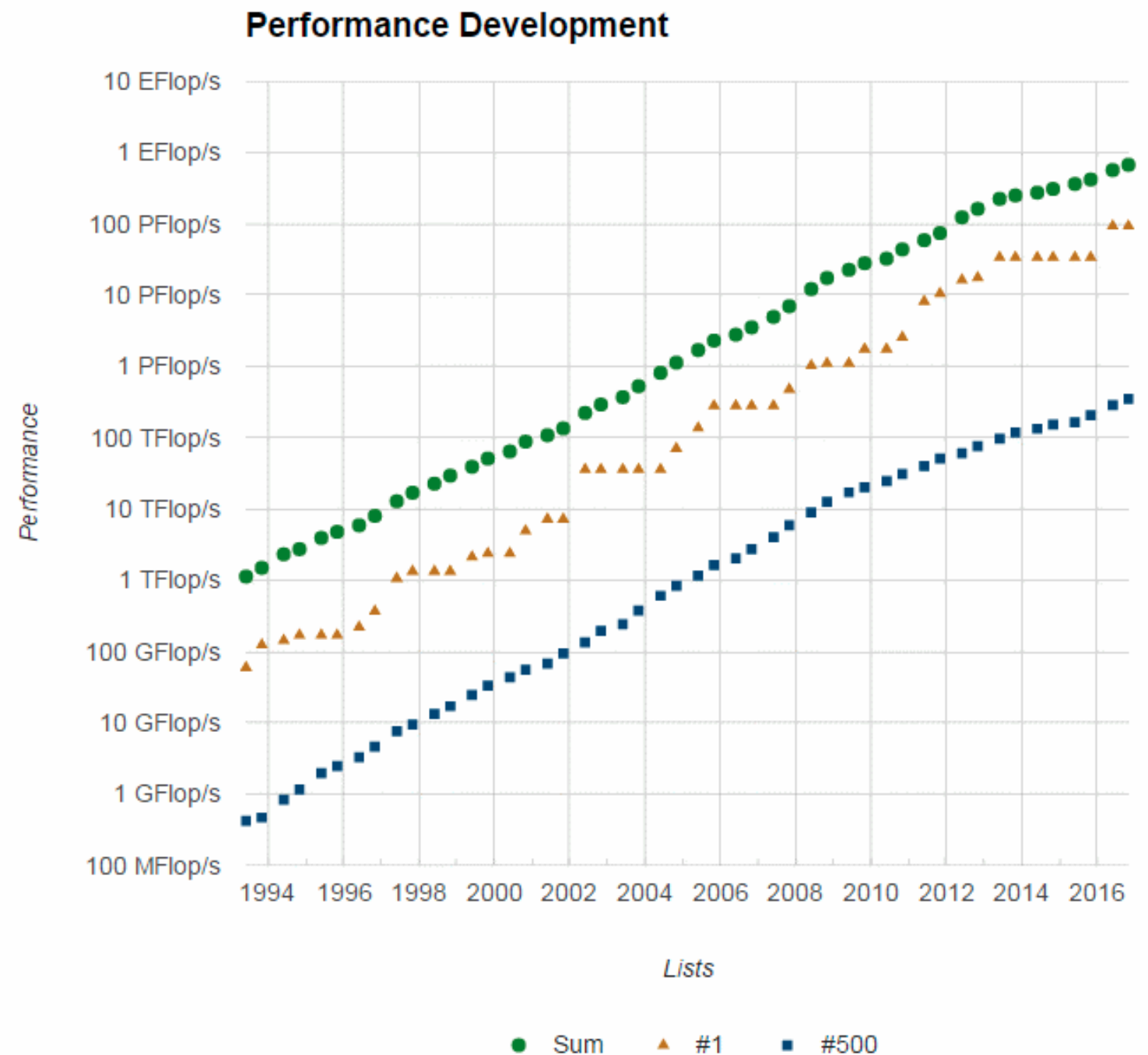
Networks *multiply* nodes into HPC clusters

- Each node is a multi-processor computer
- Multiple nodes are networked together
- Special purpose nodes, also multi-processor, are used for other purposes (i.e. GPU nodes, I/O nodes etc).



Voila!

- Development of:
 - Multi-core, multi-thread CPUs
 - Networks
 - Distributed (I/O) systems
 - GPUs
- (+ Parallel programming)



Why HPC matters

- Exact solutions are not always possible using current theoretical tools and methods
 - i.e. most problems we have to solve are non-linear
- Numerical integration and simulation techniques are providing answers to difficult problems
- The more complex the problem the more demanding the solution will be. Hence, high end research requires
 - better hardware
 - improved software stacks etc

Science will most likely impose the following..

- *“Is it possible to reduce the time it takes to solve the problem?”*
- *“Is it possible to increase the problem size?”*

IT will likely respond..

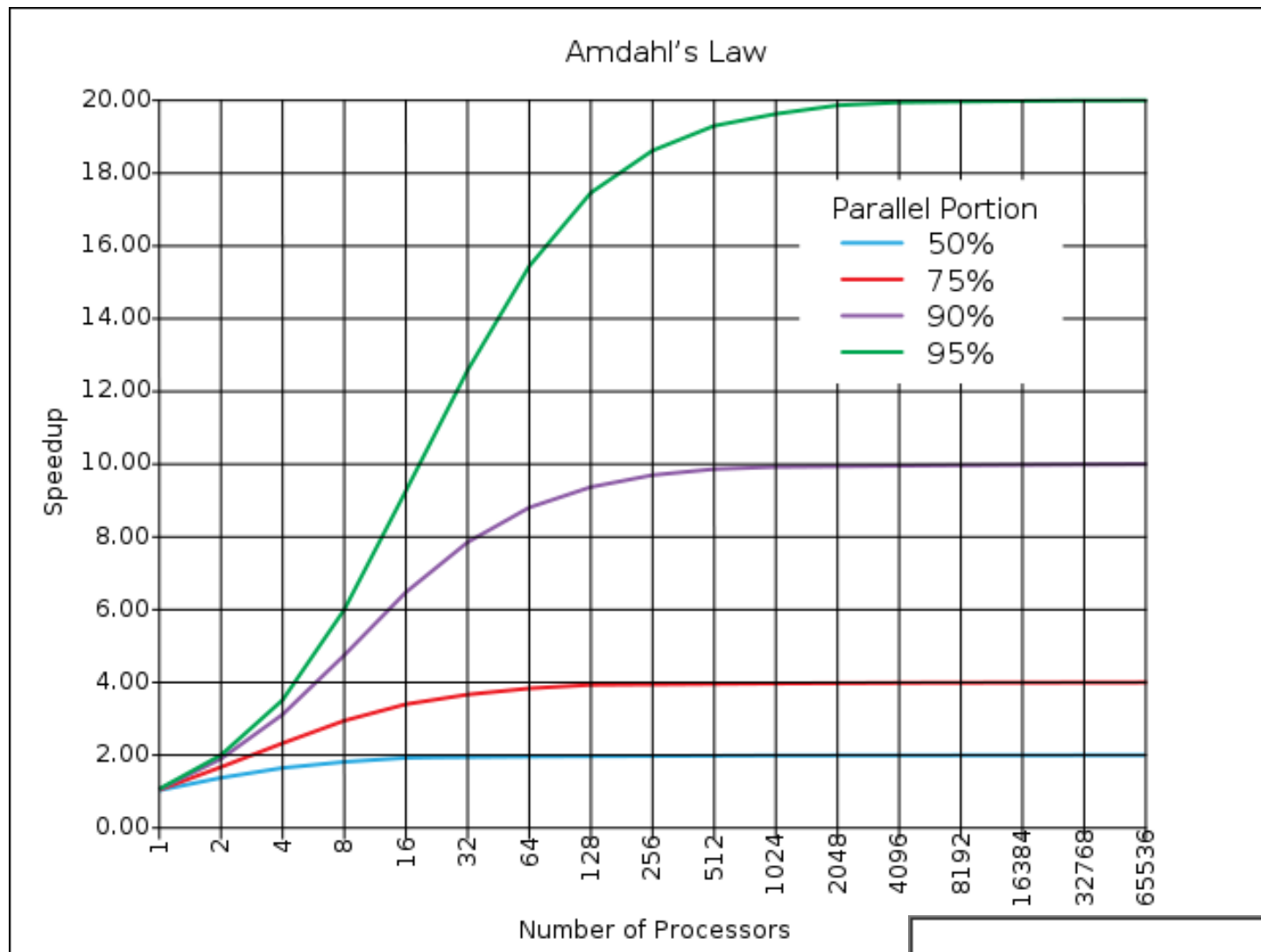
- *“Yes, a new machine is on the way...”* – **Hardware specs**
- *“Try improving your code”* – **Software refactoring**
- *“Try linking with OpenBLAS or MKL”* – **Code re-use**

Basic Concepts and terminology

- A Compute **Node** is a standalone computer
 - It has multiple {**CPU/Processor/Socket**}s
 - Each CPU has multiple **Cores**
 - Each Core may support multiple **threads**
- A parallel program consists of multiple tasks
 - Each **task** is a “serial” set of instructions
 - Parallel **tasks exchange data** and
 - Hence may need to be **synchronized** (i.e. before or after the exchange takes place)

Concepts and terminology

- **Speedup** is the wallclock of the serial version over the wallclock of the parallel version
- **Parallel overhead** is the extra overhead (amount of time) needed to build up the parallel execution environment
- **Scalability** is the ability of a given code to demonstrate speedup with the addition of more resources.

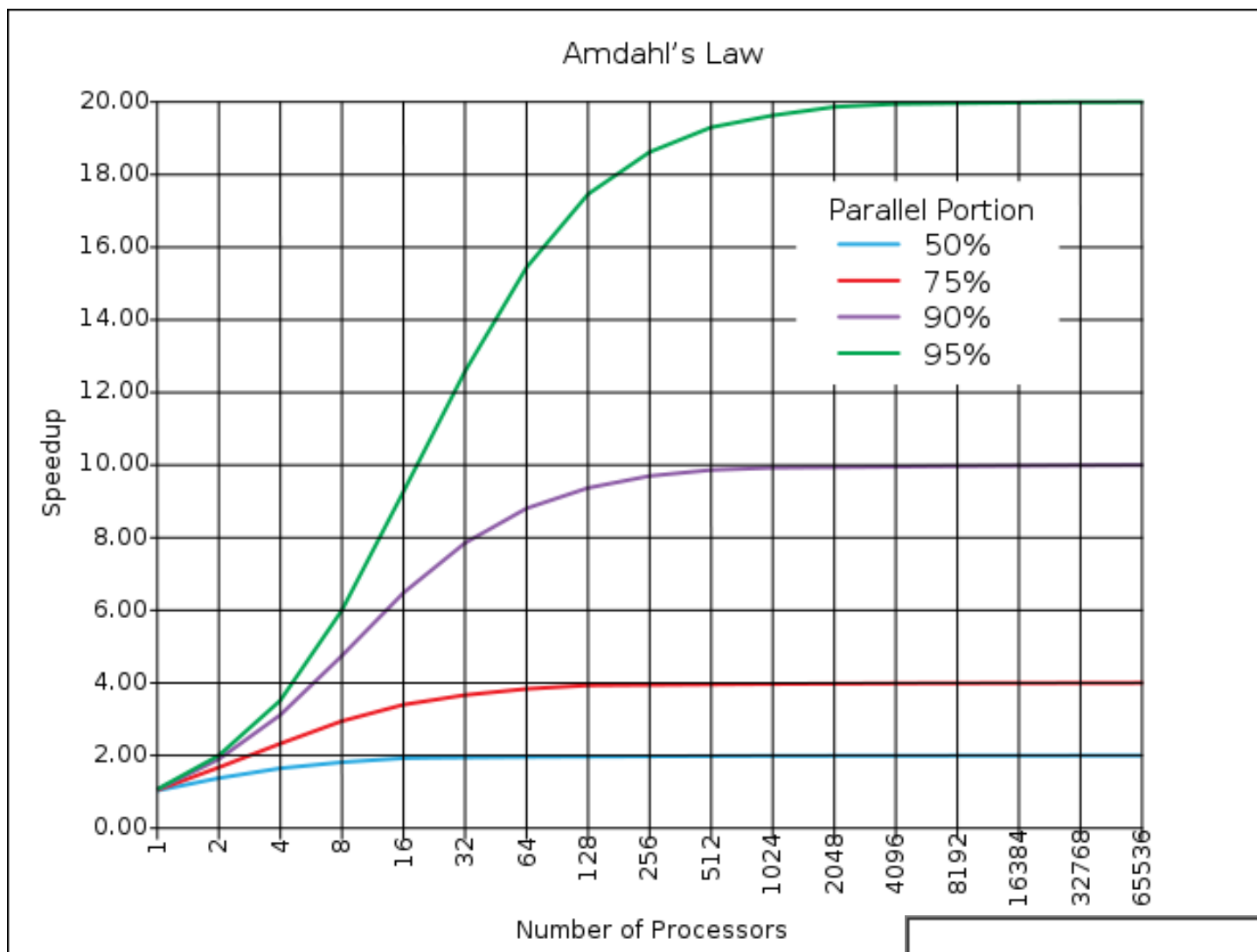


Amdahl's Law

Amdahl's law predicts the theoretical maximum speedup when using multiple processors



N	speedup			
	P = .50	P = .90	P = .95	P = .99
10	1.82	5.26	6.89	9.17
100	1.98	9.17	16.80	50.25
1,000	1.99	9.91	19.62	90.99
10,000	1.99	9.91	19.96	99.02
100,000	1.99	9.99	19.99	99.90



However, by increasing the problem size, the non-parallel segment can be reduced

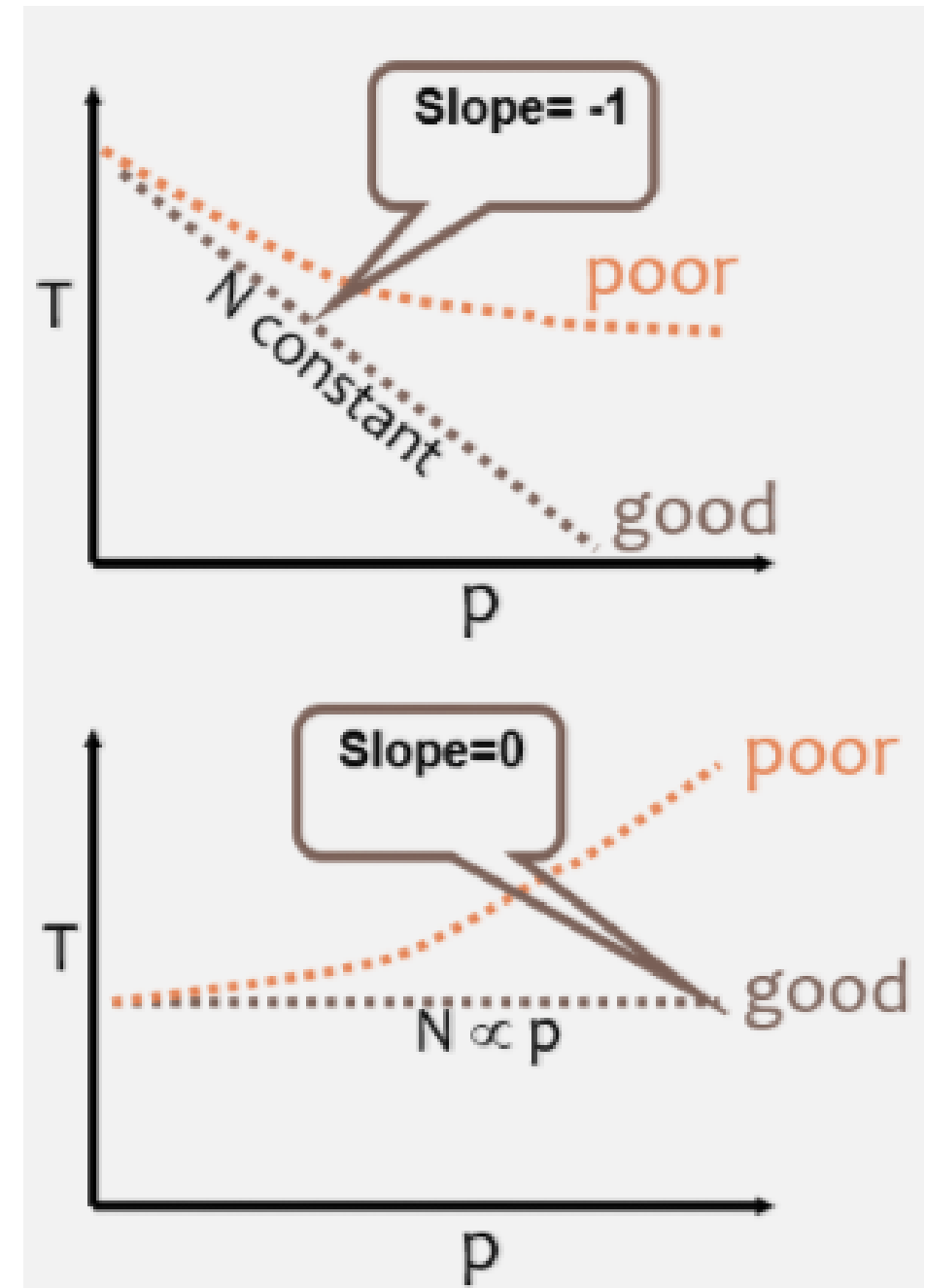
Problems that increase the percentage of parallel time with their size are more scalable than problems with a



N	speedup			
	P = .50	P = .90	P = .95	P = .99
10	1.82	5.26	6.89	9.17
100	1.98	9.17	16.80	50.25
1,000	1.99	9.91	19.62	90.99
10,000	1.99	9.91	19.96	99.02
100,000	1.99	9.99	19.99	99.90

Scalability

- Strong scaling
 - Problem size is fixed
 - Goal is to solve faster
 - Perfect scaling means speedup is $\sim P$
- Weak scaling
 - Problem size per processor is fixed
 - Goal is to run a larger problem in the same unit of time
 - Perfect scaling means the larger problem is solved in the same unit of time

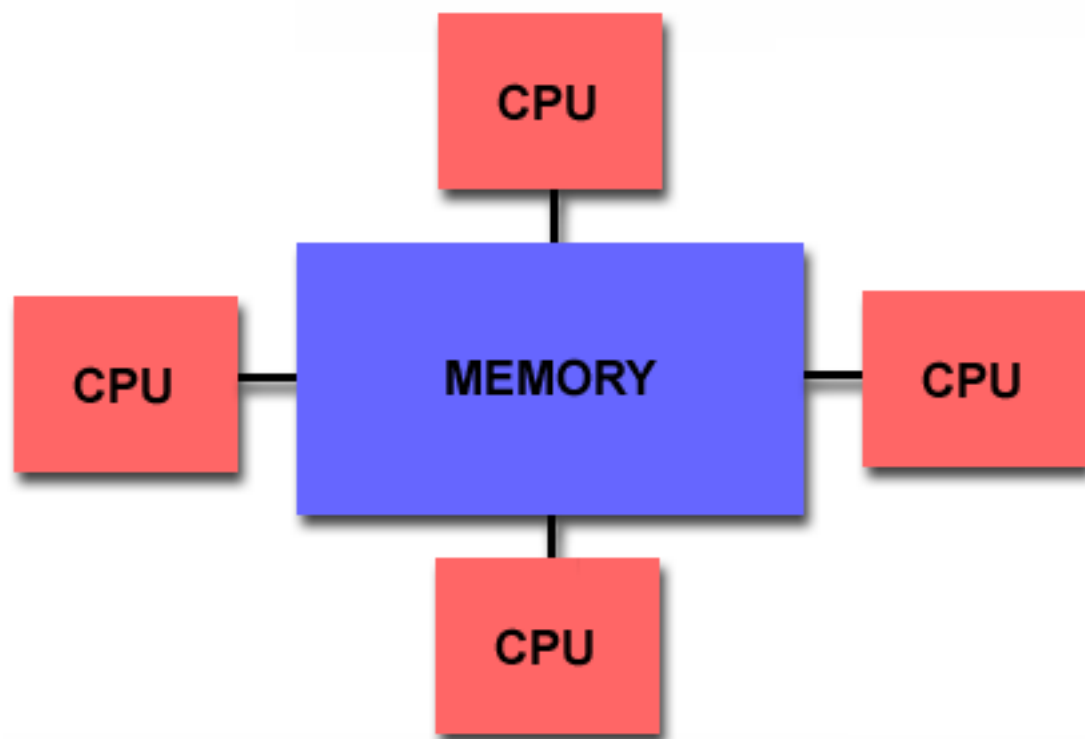


One final note...

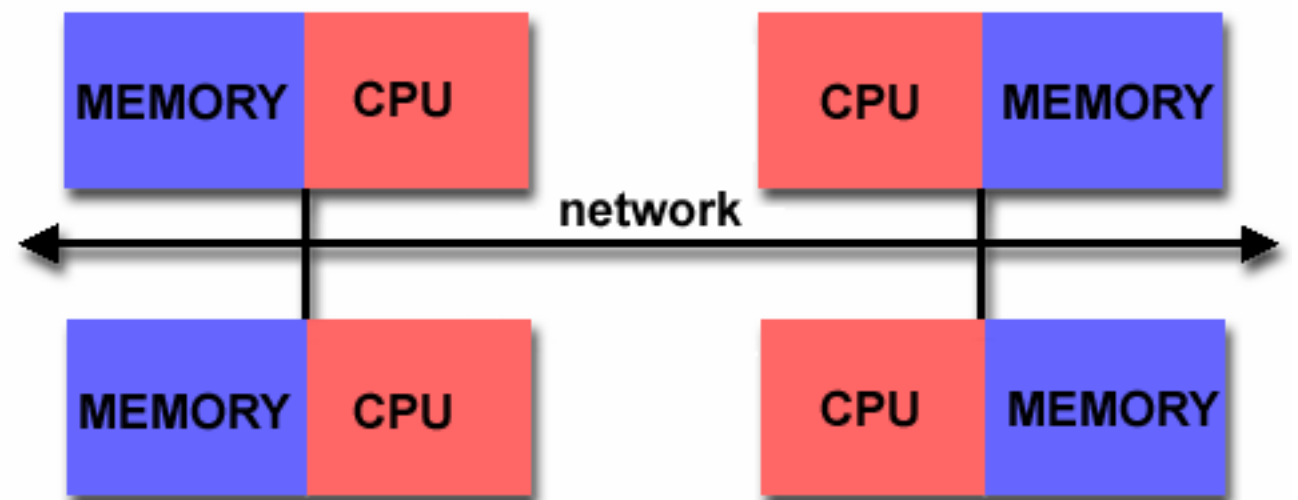
- Parallel programming may overcome the issues but before doing anything parallel make sure that:
 - Your serial code is already optimized! Questions to ask yourself:
 - *Are you using other people's computational and I/O libraries?*
 - *Have you tested with other compilers and, if yes, have you tried various optimization flags?*
 - *What does profiling tell you?*

Parallel programming models

Shared memory



Distributed memory



Parallel programming models

Shared memory

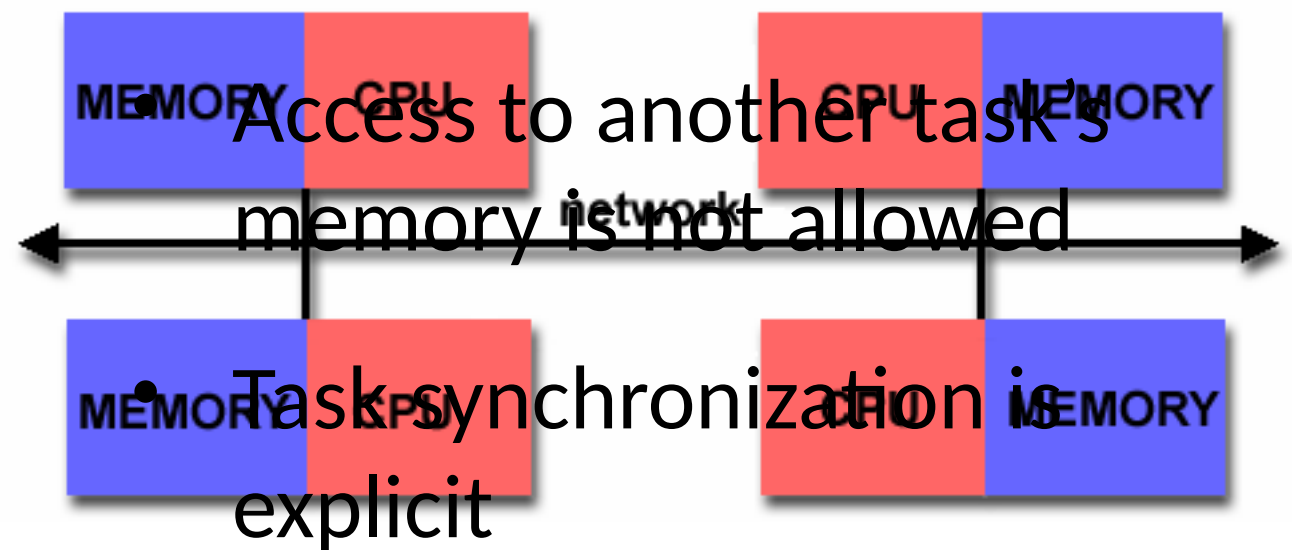
- Each **thread** shares the same address space with other threads



- Threads synchronization is implicit
- Not scalable

Distributed memory

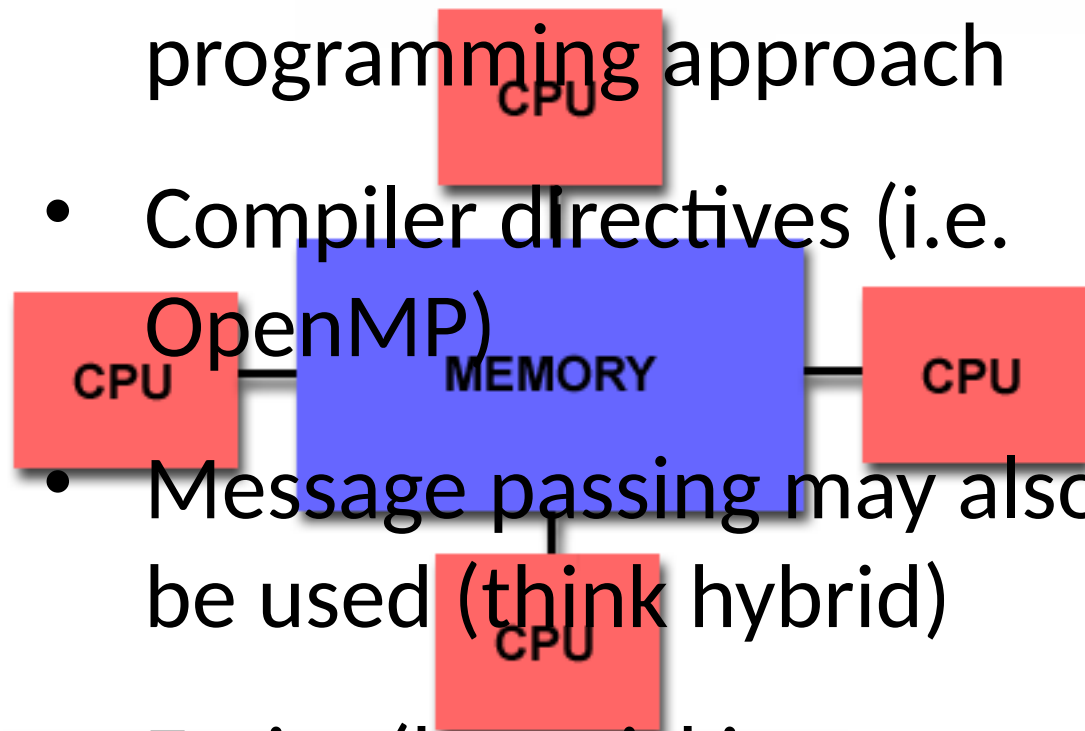
- Each **task** has access to a unique address space



Parallel programming models

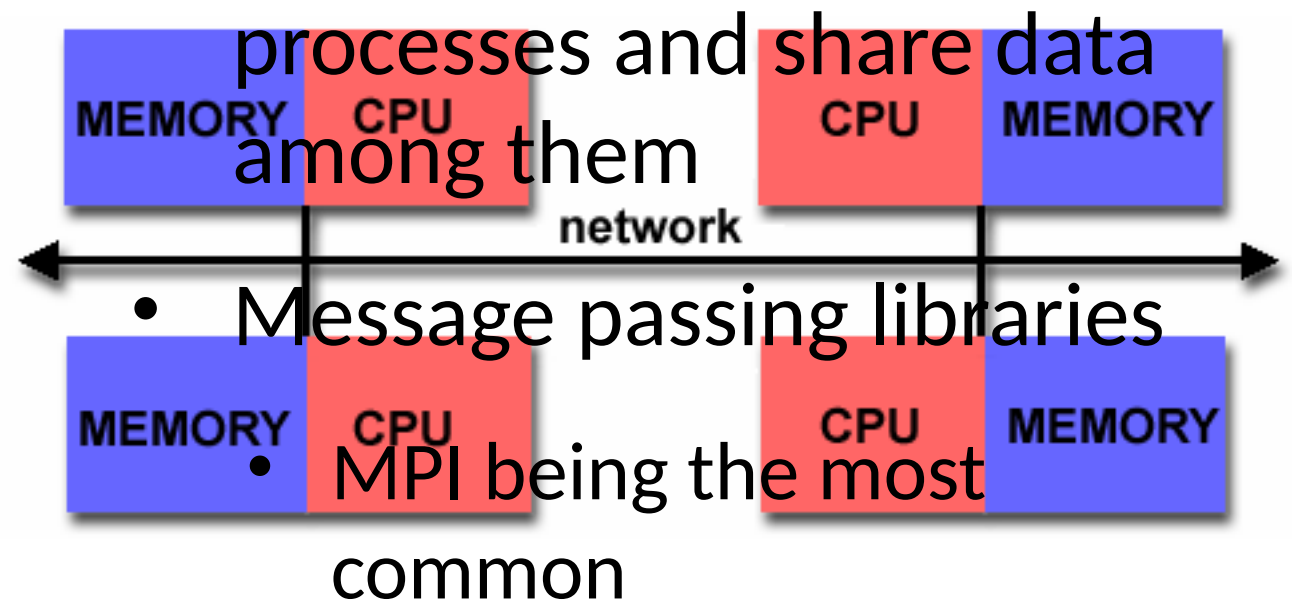
Shared memory

- Thread based programming approach
- Compiler directives (i.e. OpenMP)
- Message passing may also be used (think hybrid)
- Easier (but trickier sometimes) to implement



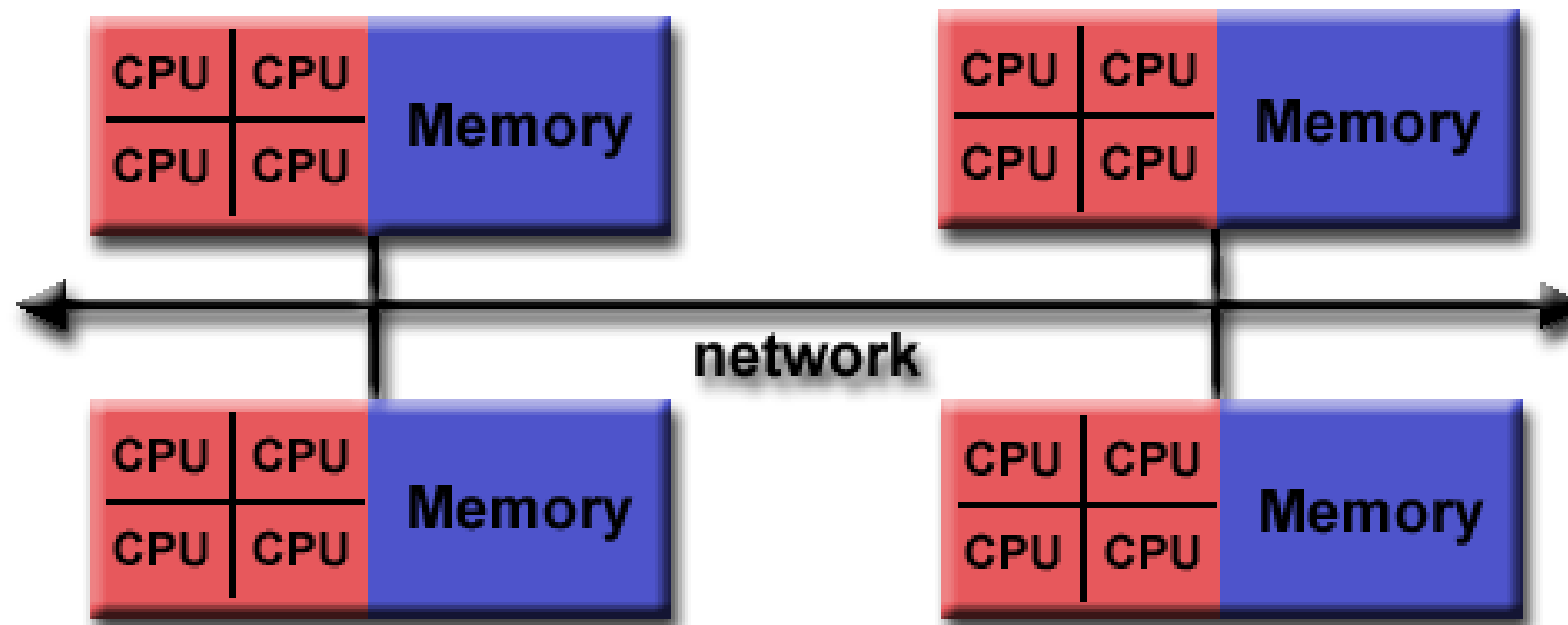
Distributed memory

- Developer uses “Message Passing” in order to sync



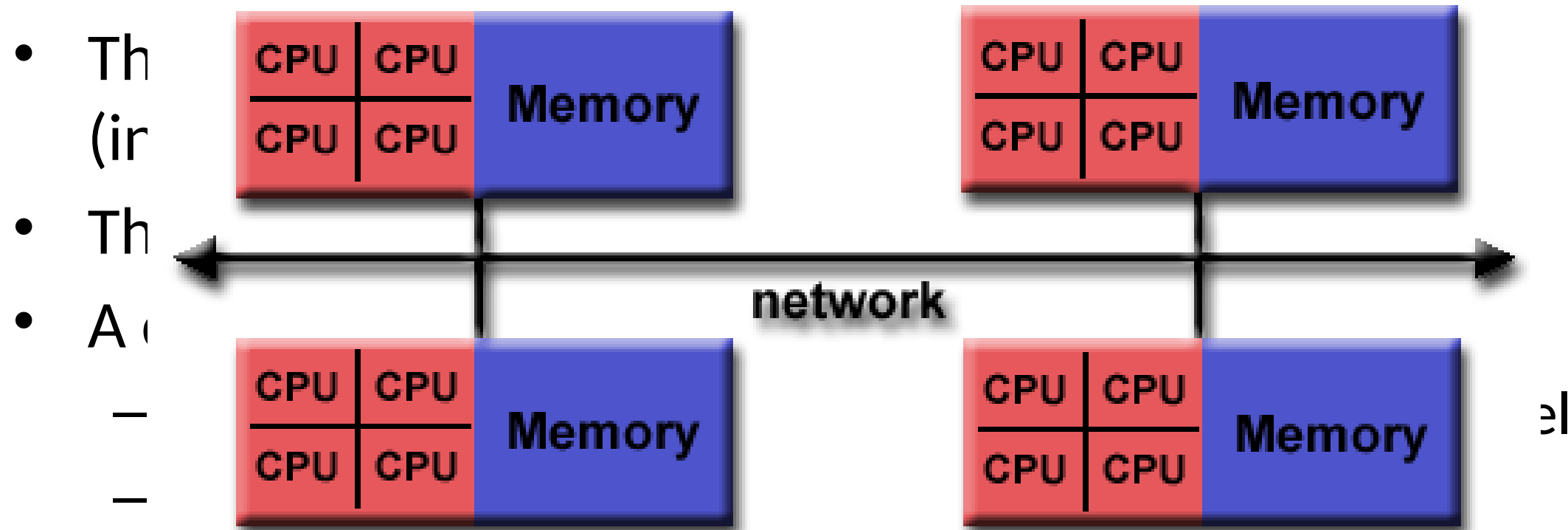
- Difficult to implement

Hybrid Distributed-Shared memory



Hybrid Distributed-Shared memory

- Most (all?) HPC systems currently employ both shared and distributed memory architectures



Designing parallel programs

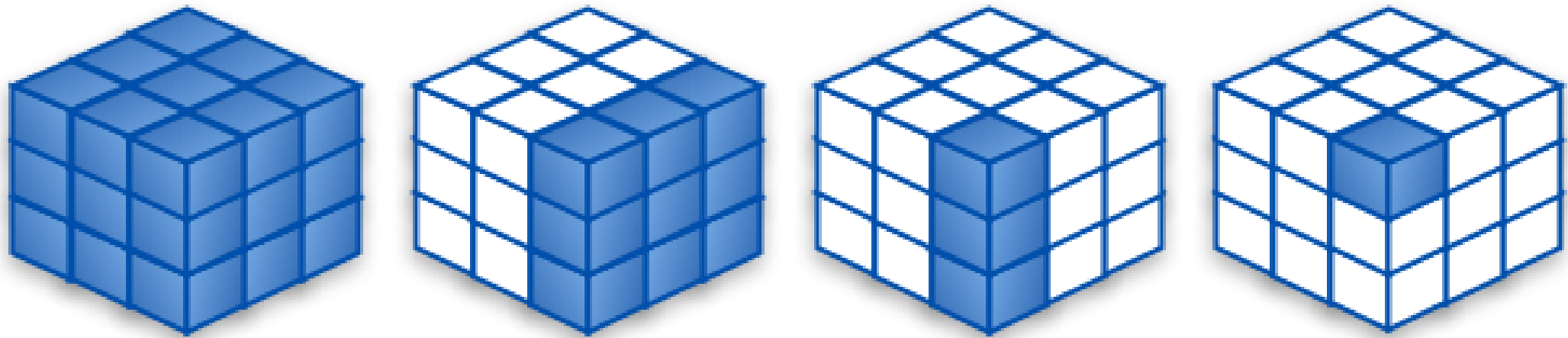
- First step: Understand the problem
 - Before beginning make sure the serial only version is already at its best
 - For example take advantage of optimized libraries such as OpenBLAS or MKL
 - Investigate if (and if yes, how) the program can be parallelized
- Profile the serial program's runtime
 - Where is time mostly being spent
 - Focus on those parts
 - Identify potential bottlenecks (i.e. I/O steps)

Nature of the problem

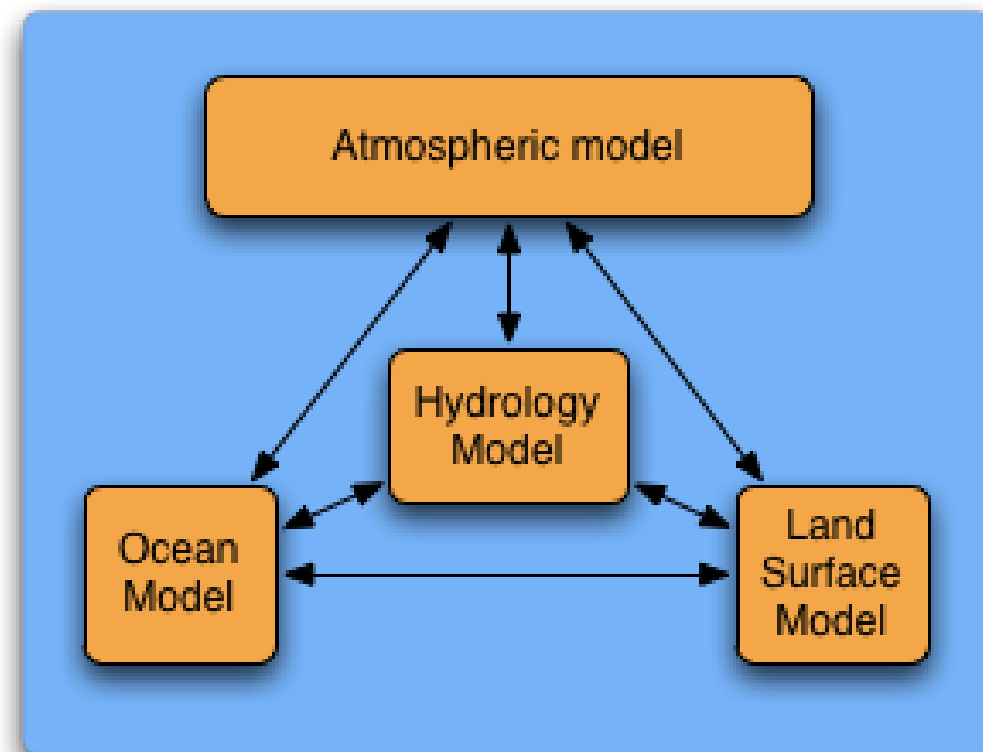


Nature of the problem (examples)

- Domain decomposition

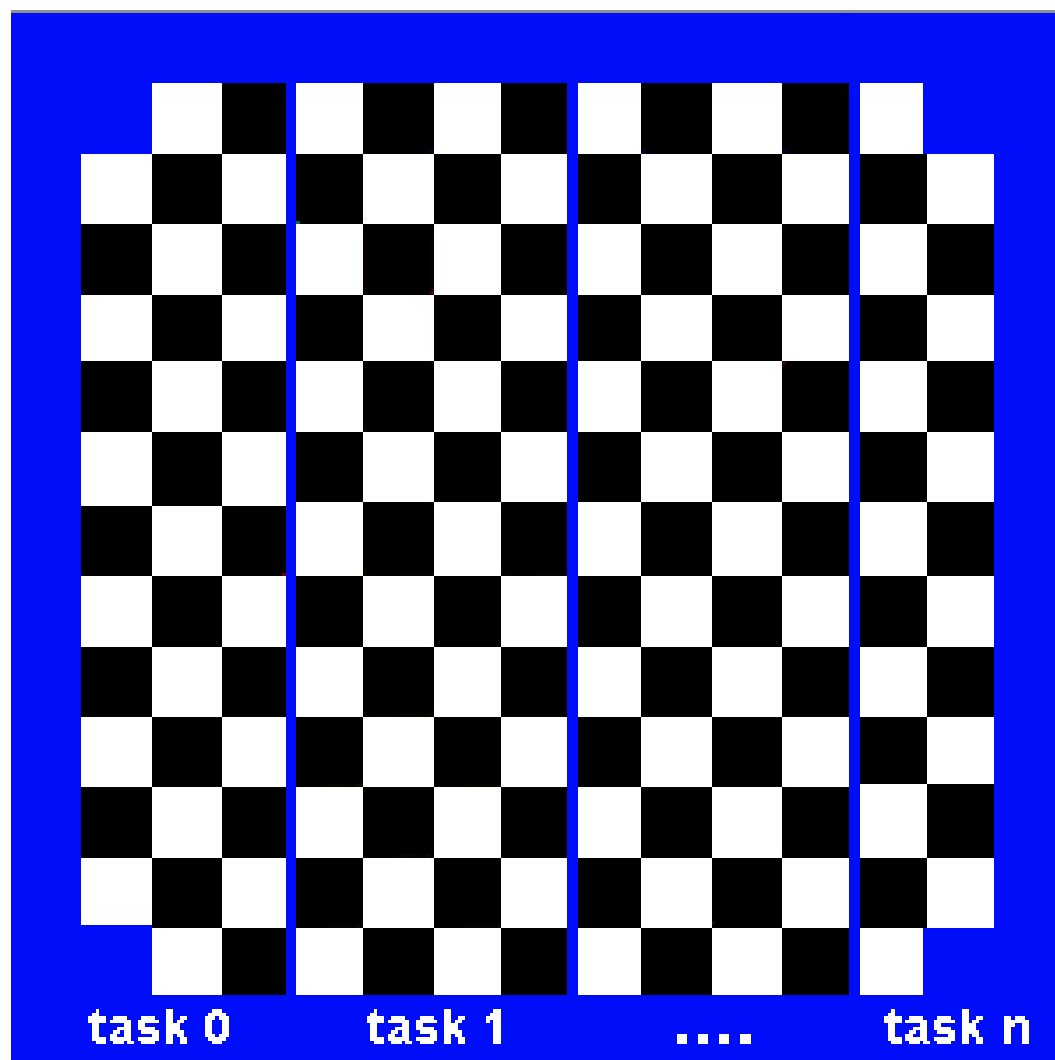


- Functional partitioning

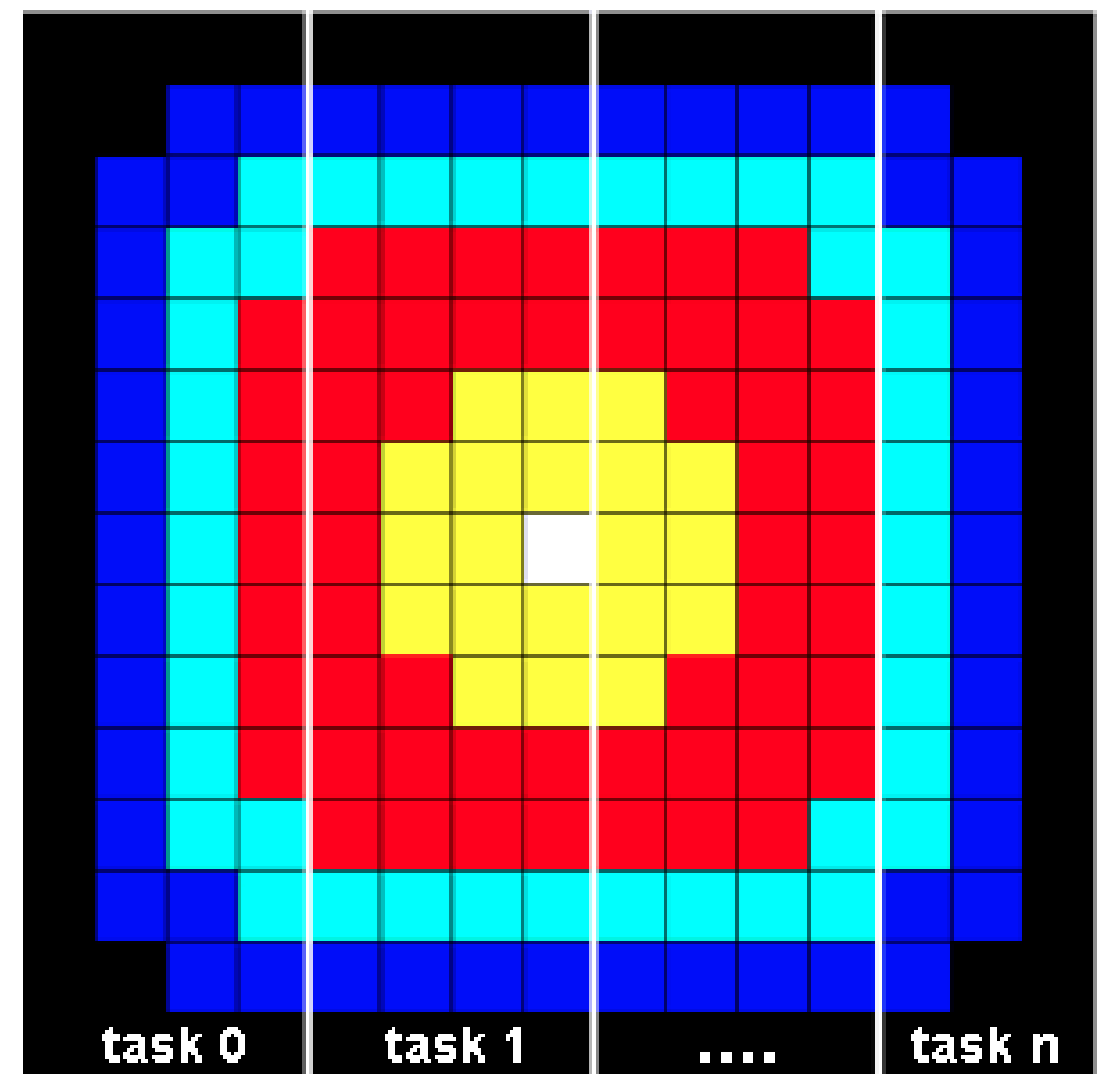


Communications (domain decomposition)

- Rendering a 2D image



- Explicit 2D scheme



Communications Overhead

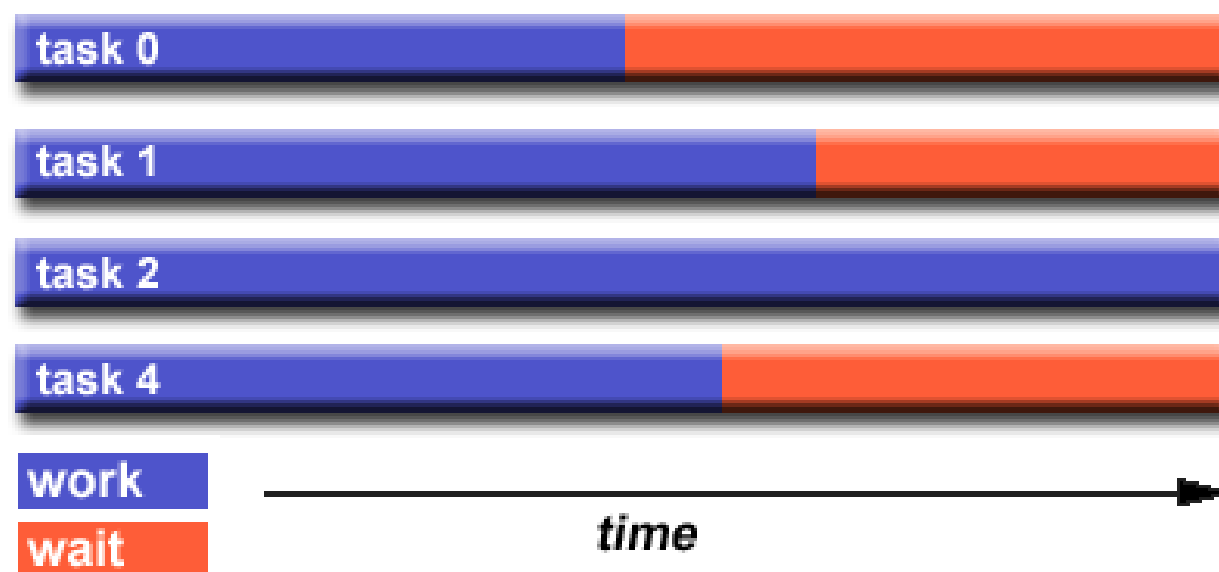
- Communications induce (inevitably) parallel overheads
 - CPU Cycles are used to dispatch/receive data
 - Points of synchronization need to be introduced
 - Traffic may saturate the available network bandwidth
- Modes of communication
 - Synchronous (or blocking)
 - Asynchronous (or non-blocking)
 - Used to overlap computation with communication in order not to waste CPU Cycles
- Efficiency of communications depends mostly on
 - MPI (or other protocol) Implementation being used
 - Network fabric

Synchronization types

- Barriers
 - All tasks are involved
 - All wait until the last (slowest) task reaches the barrier
- All synchronous communications
 - Collective ones are hence implicitly barriers
- Locks
 - May involve any number of parallel tasks
 - Used to protect a code segment from being executed in parallel (i.e. increments)
 - Can be blocking or non-blocking

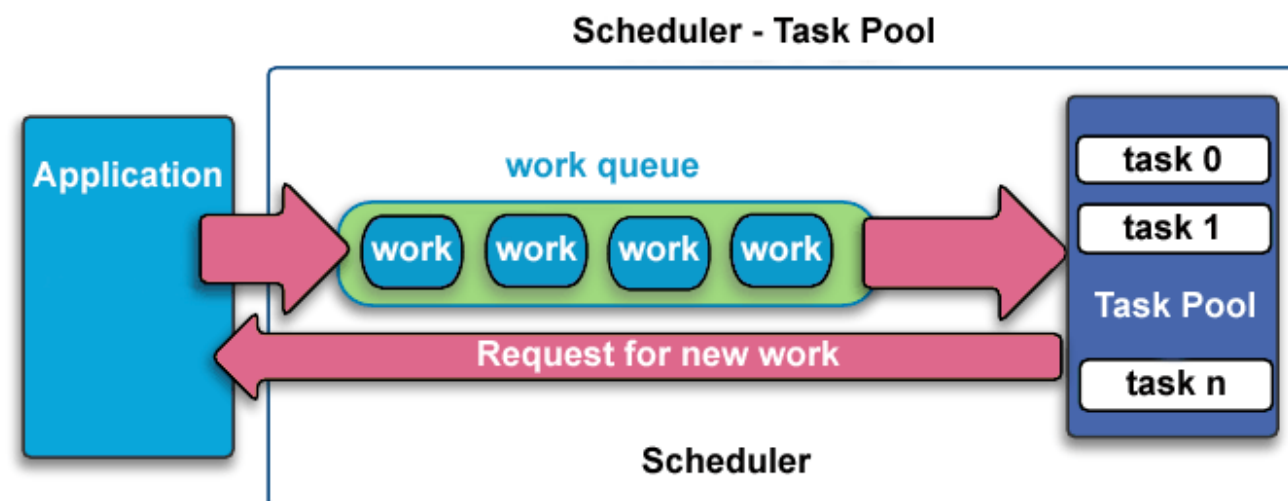
Load balancing

- The practice of
 - distributing approximately equal amount of work to all tasks
 - Minimizing idle time
- The slowest (most loaded) task determines the overall performance



Common approaches

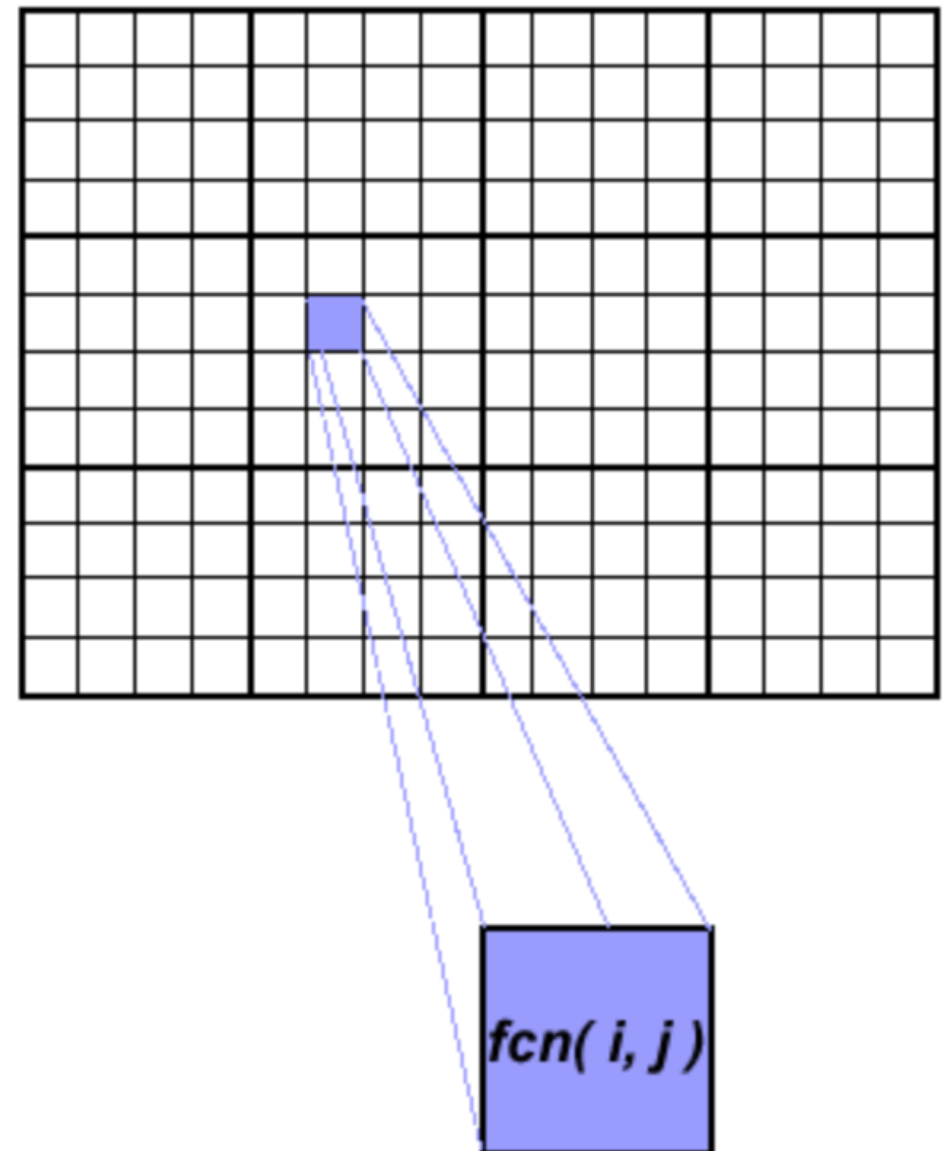
- Equally partition the work (whenever possible)
- But under circumstances this cannot be done beforehand
 - For example: Sparse linear algebra, adaptive mesh refinement and other use cases
 - In such cases we use dynamic scheduling of small chunks of workloads
 - Each task picks up a workload and requests a new one upon completion



Example - 2D Array

- Calculation of array elements

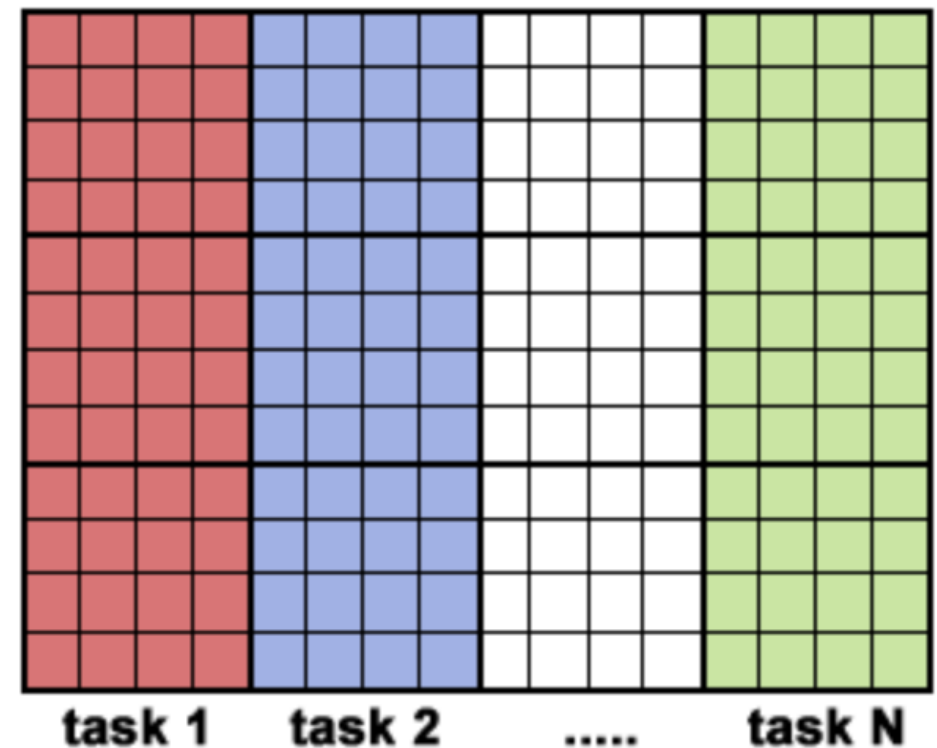
```
do j = 1,n
  do i = 1,n
    a(i,j) = fcn(i,j)
  end do
end do
```



Example – 2D Array

- Calculation of array elements

```
do j = mystart, myend  
  do i = 1, n  
    a(i,j) = fcn(i,j)  
  end do  
end do
```



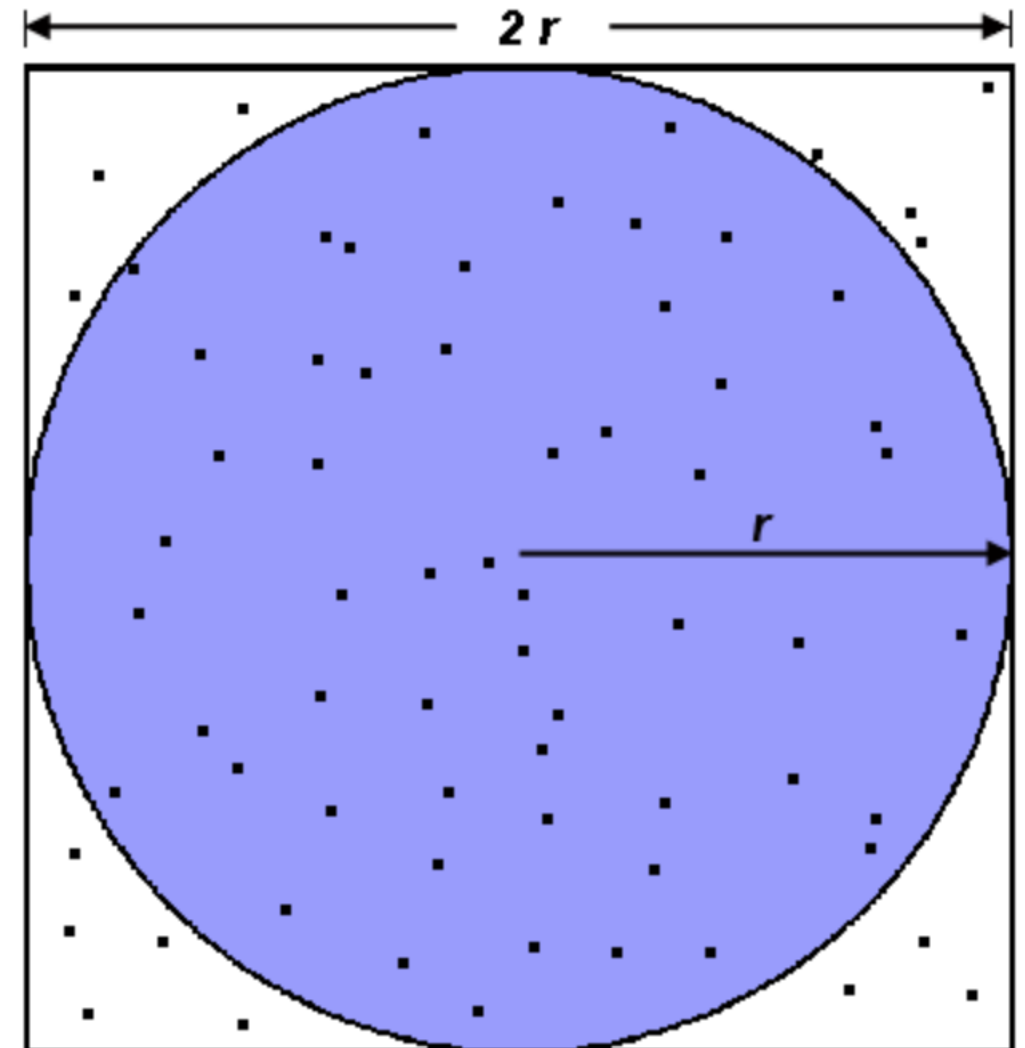
Example – Pi calculation

- Serial pseudo-code:

```
npoints = 10000
circle_count = 0

do j = 1, npoints
  generate 2 random numbers between 0 and 1
  xcoordinate = random1
  ycoordinate = random2
  if (xcoordinate, ycoordinate) inside circle
  then circle_count = circle_count + 1
end do

PI = 4.0 * circle_count / npoints
```



$$A_s = (2r)^2 = 4r^2$$
$$A_c = \pi r^2$$
$$\pi = 4 \times \frac{A_c}{A_s}$$

Example – Pi calculation

- Modified pseudo-code:

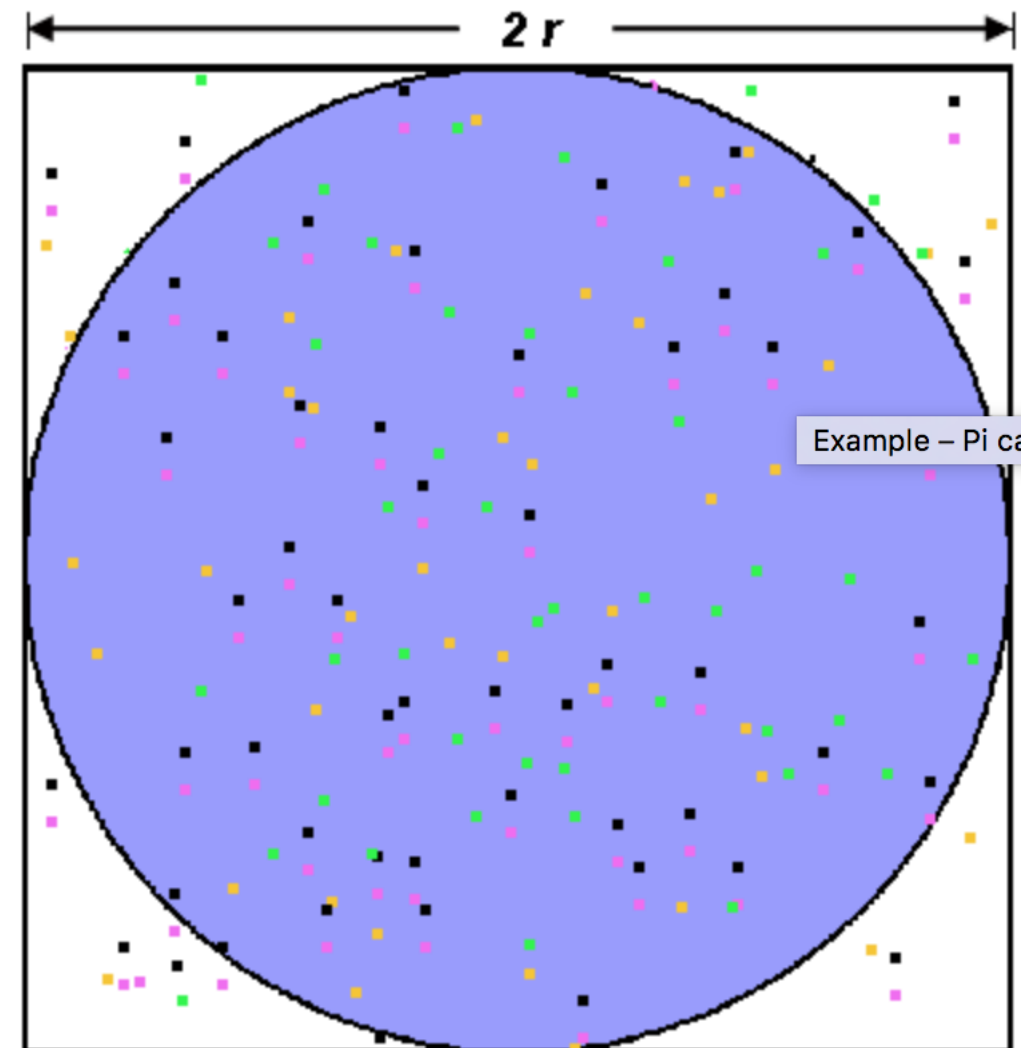
```

npoints = 10000
circle_count = 0

p = number of tasks
num = npoints/p

do j = 1,num
  generate 2 random numbers between 0 and 1
  xcoordinate = random1
  ycoordinate = random2
  if (xcoordinate, ycoordinate) inside circle
  then circle_count = circle_count + 1
end do

PI = 4.0*circle_count/npoints
  
```

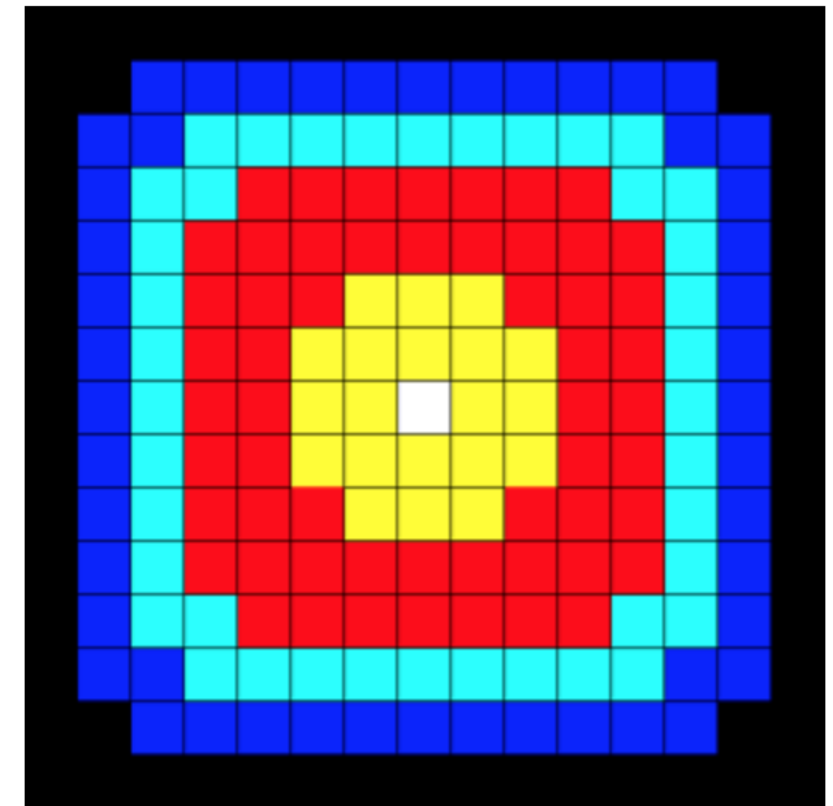


$$\begin{aligned}
 A_S &= (2r)^2 = 4r^2 \\
 A_C &= \pi r^2 \\
 \pi &= 4 \times \frac{A_C}{A_S}
 \end{aligned}$$

Example - 2D heat equation

- Calculation depends upon neighboring grid points

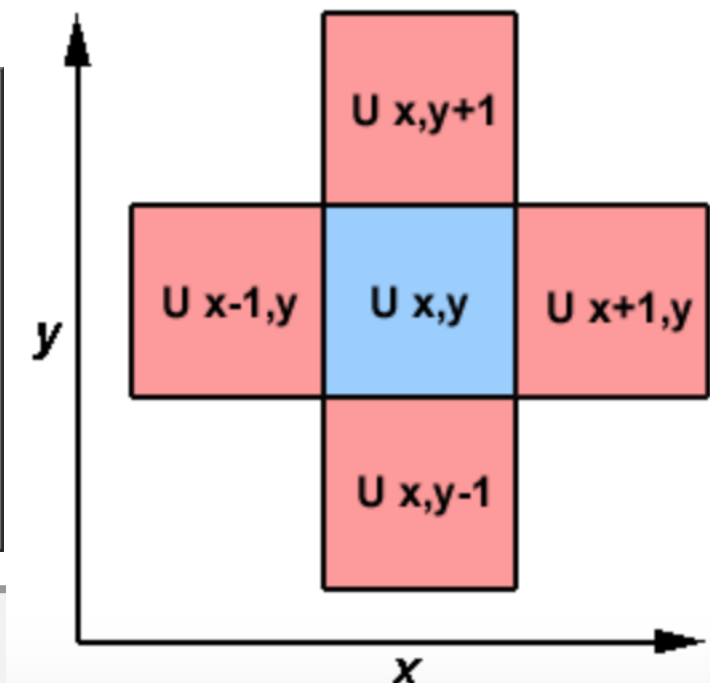
$$\begin{aligned}
 U_{x,y} = & U_{x,y} \\
 & + C_x * (U_{x+1,y} + U_{x-1,y} - 2 * U_{xy}) \\
 & + C_y * (U_{x,y+1} + U_{x,y-1} - 2 * U_{x,y})
 \end{aligned}$$



- Serial pseudo-code:

```

do iy = 2, ny - 1
  do ix = 2, nx - 1
    u2(ix, iy) = u1(ix, iy) +
      cx * (u1(ix+1,iy) + u1(ix-1,iy) - 2.*u1(ix,iy)) +
      cy * (u1(ix,iy+1) + u1(ix,iy-1) - 2.*u1(ix,iy))
  end do
end do
  
```



Example - 2D heat equation

- Modified pseudo-code:

```

find out if I am MASTER or WORKER

if I am MASTER
  initialize array
  send each WORKER starting info and subarray
  receive results from each WORKER

else if I am WORKER
  receive from MASTER starting info and subarray

  # Perform time steps
  do t = 1, nsteps
    update time
    send neighbors my border info
    receive from neighbors their border info
    update my portion of solution array

  end do

  send MASTER results

endif
  
```

